



# An Application of Intuitionistic Pentagonal Fuzzy Relation in Medical Diagnosis

Research Article\*

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**Abstract:** In this paper, we study Sanchez's method of medical diagnosis by using Intuitionistic Pentagonal Fuzzy Relation. To develop Intuitionistic Pentagonal Fuzzy Relation and using score and accuracy function for to solve medical diagnosis decision making problem. In this paper it is presented the procedures based on Intuitionistic Pentagonal Fuzzy Number for medical diagnosis using a numerical example to verify the proposed approach.

**Keywords:** Medical Diagnosis, Intuitionistic Pentagonal Fuzzy Relation, Score, Accuracy.

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## 1. Introduction

In this chapter, a system for medical diagnosis based on Pentagonal Valued Intuitionistic Fuzzy Relation is proposed. The Intuitionistic Fuzzy Sets [IFSs] were first introduced by Atanassov (1986) which is a generalization of the concept of fuzzy set by Zadeh (1965). The basic characteristic of the IFS is that the values of its membership function and non membership function are intervals rather than exact numbers. Shannon et al. were the first to develop an approach using IFS for decision making in medical diagnosis. In this chapter, Pentagonal Valued Intuitionistic Fuzzy Relation is used to solve medical diagnosis decision making problem. We study Sanchez's method of medical diagnosis with the notion of PVIFS. Numerical examples are provided to illustrate these approaches.

## 2. Basic Definitions

**Definition 2.1** (Fuzzy Number). A Fuzzy Number  $\tilde{A}$  is a fuzzy set on the real line  $R$  must satisfy the following conditions.

1.  $\mu_{\tilde{A}}(x_0)$  is piecewise continuous.
2. There exists at least one  $x_0 \in R$  with  $\mu_{\tilde{A}}(x_0) = 1$ .
3.  $\tilde{A}$  must be normal and convex.

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**Definition 2.2** (Pentagonal Fuzzy Number). A *Pentagonal Fuzzy Number (PFN)* of a fuzzy set  $\tilde{A}$  is defined as  $\tilde{A}_P = (a, b, c, d, e)$  and its membership function is given by,

$$\mu_{\tilde{A}_P} = \begin{cases} 0, & \text{for } x < a \\ \frac{x-a}{(b-a)}, & \text{for } a \leq x \leq b \\ \frac{(x-b)}{(c-b)}, & \text{for } b \leq x \leq c \\ 1, & \text{for } x = c \\ \frac{(d-x)}{(d-c)}, & \text{for } c \leq x \leq d \\ \frac{(e-x)}{(e-d)}, & \text{for } d \leq x \leq e \\ 0, & \text{for } x > e \end{cases}$$

**Definition 2.3** (Operations on Pentagonal Fuzzy Number). Let  $A = (a_1, b_1, c_1, d_1, e_1)$  and  $B = (a_2, b_2, c_2, d_2, e_2)$  be two PFN (*Pentagonal Fuzzy Number*) then min and max operator for any two PFNs are defined as,

$$\begin{aligned} \min(A, B) &= (\min(a_1, a_2), \min(b_1, b_2), \min(c_1, c_2), \min(d_1, d_2), \min(e_1, e_2)) \\ \max(A, B) &= (\max(a_1, a_2), \max(b_1, b_2), \max(c_1, c_2), \max(d_1, d_2), \max(e_1, e_2)) \end{aligned}$$

*Supremum of PFN:* Let  $A = (x_1, x_2, x_3, x_4, x_5)$  be a PFN, then *Sup* ( $A$ ) is defined as  $\sup(A) = x_5$ .

**Definition 2.4** (Intuitionistic Fuzzy Set). Let  $X$  denote a universe of discourse, then the intuitionistic fuzzy set  $A$  in  $X$  is given by,  $\tilde{A}_I = \{ \langle x, \mu_{\tilde{A}}(x), \nu_{\tilde{A}}(x) \rangle / x \in C \}$ , where  $\mu_{\tilde{A}} : x \rightarrow [0, 1]$  and  $\nu_{\tilde{A}} : x \rightarrow [0, 1]$  with the condition  $0 \leq \mu_{\tilde{A}}(x) + \nu_{\tilde{A}}(x) \leq 1, x \in X$ . Here  $\mu_{\tilde{A}}(x)$  and  $\nu_{\tilde{A}}(x) \in [0, 1]$  denote the membership and the non membership function of the fuzzy set  $A$ .

**Definition 2.5** (Intuitionistic Fuzzy Number). An *Intuitionistic Fuzzy Set*  $\tilde{A}_I$  is called an *Intuitionistic Fuzzy Number* if it satisfies the following conditions,

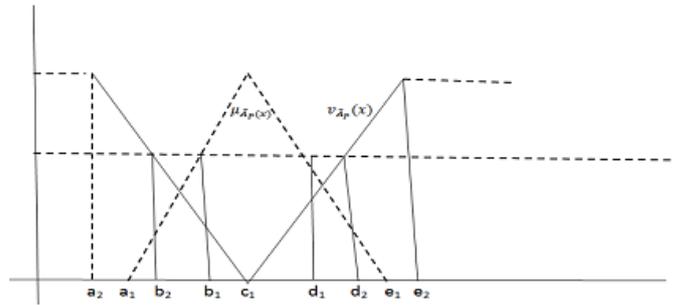
1.  $\tilde{A}_I$  is normal, (i.e) there exists at least two points  $x_0, x_1 \in X$  such that  $\mu_{\tilde{A}}(x_0) = 1$  and  $\nu_{\tilde{A}}(x_0) = 1$ .
2.  $\tilde{A}_I$  is convex, (i.e) its membership function is fuzzy convex and its non membership function is concave.
3. Its membership function is upper semicontinuous and its non membership function is lower semicontinuous and the set  $\tilde{A}_I$  is bounded.

**Definition 2.6** (Intuitionistic Pentagonal Fuzzy Number). An *Intuitionistic Pentagonal Fuzzy Number* of a *Intuitionistic Fuzzy Number (IFS)* is  $\tilde{A}_I$  is defined as  $\tilde{A}_{IP} = \{(a_1, b_1, c_1, d_1, e_1)(a_2, b_2, c_2, d_2, e_2)\}$  where all  $(a_1, b_1, c_1, d_1, e_1)(a_2, b_2, c_2, d_2, e_2)$  are real number and its membership function  $\mu_{\tilde{A}_{IP}}(x)$ , non-membership function  $\nu_{\tilde{A}_{IP}}(x)$  are given by

$$\mu_{\tilde{A}_{IP}} = \begin{cases} 0, & \text{for } x < a_1 \\ \frac{(x-a_1)}{(b_1-a_1)}, & \text{for } a_1 \leq x \leq b_1 \\ \frac{(x-b_1)}{(c_1-b_1)}, & \text{for } b_1 \leq x \leq c_1 \\ 1, & \text{for } x = c_1 \\ \frac{(d_1-x)}{(d_1-c_1)}, & \text{for } c_1 \leq x \leq d_1 \\ \frac{(e_1-x)}{(e_1-d_1)}, & \text{for } d_1 \leq x \leq e_1 \\ 0, & \text{for } x > e_1 \end{cases}$$

$$\mu_{\tilde{A}P} = \begin{cases} 0, & \text{for } x < a_2 \\ \frac{(x-a_2)}{(b_2-a_2)}, & \text{for } a_2 \leq x \leq b_2 \\ \frac{(x-b_2)}{(c_2-b_2)}, & \text{for } b_2 \leq x \leq c_2 \\ 1, & \text{for } x = c_2 \\ \frac{(d_2-x)}{(d_2-c_2)}, & \text{for } c_2 \leq x \leq d_2 \\ \frac{(e_2-x)}{(e_2-d_2)}, & \text{for } d_2 \leq x \leq e_2 \\ 0, & \text{for } x > e_2 \end{cases}$$

**Definition 2.7.** Graphical representation of Intuitionistic Pentagonal Fuzzy Number (IPFN)



**Definition 2.8** (Score function of an Intuitionistic Pentagonal Fuzzy Number). Score function of an Intuitionistic Pentagonal Fuzzy Number  $\tilde{A}_{IP} = \{(a_1, b_1, c_1, d_1, e_1)(a_2, b_2, c_2, d_2, e_2)\}$  is defined as,  $S(\tilde{A}_{IP}) = \frac{(a_1 - a_2 + b_1 - b_2 + c_1 - c_2 + d_1 - d_2 + e_1 - e_2)}{5}$  where  $S(\tilde{A}_{IP}) \in [-1, 1]$ .

**Definition 2.9** (Accuracy Function of an IPFN). A accuracy function of an Intuitionistic Pentagonal Fuzzy Number  $\tilde{A}_{IP} = \{(a_1, b_1, c_1, d_1, e_1)(a_2, b_2, c_2, d_2, e_2)\}$  is defined as,  $S(\tilde{A}_{IP}) = \frac{(a_1 + a_2 + b_1 + b_2 + c_1 + c_2 + d_1 + d_2 + e_1 + e_2)}{5}$  where  $H(\tilde{A}_{IP}) \in [-1, 1]$ . The Score function  $S$  and the Accuracy function  $H$  are respectively, defined as the difference and sum of the membership function  $\mu_{\tilde{A}_{IP}}(x)$ , non-membership function  $\nu_{\tilde{A}_{IP}}(x)$ .

**Definition 2.10** (Pentagonal Valued Intuitionistic Fuzzy Relation). We defined Pentagonal Valued Intuitionistic Fuzzy Relations and Composition of fuzzy relation.

**Definition 2.11.** Let  $X$  and  $Y$  be two sets. A Pentagonal Valued Intuitionistic Fuzzy Relation (PVIFR)  $R$  from  $X$  to  $Y$  is a PVIFR of  $X \times Y$  characterized by the membership function  $\mu_R$  and non-membership function  $\nu_R$  where out put value of  $\mu_R$  and  $\nu_R$  is a pentagonal fuzzy number. A PVIFR  $R$  from  $X$  to  $Y$  will be denoted by  $R(X \rightarrow Y)$ .

**Definition 2.12.** If  $A$  is an PVIFS of  $X$ , the Composition of the Pentagonal Valued Intuitionistic Fuzzy Relation  $R(X \rightarrow Y)$  with  $A$  is a PVIFS  $B$  of  $Y$  denoted by  $B = R \circ A$ , and is defined as  $R \circ A(y) = (\mu_{R \circ A}(y), \nu_{R \circ A}(y)) = B(y)$  where  $\mu_{R \circ A}(y) = \max[\mu_A(x) \min \mu_R(x, y)]$  and  $\nu_{R \circ A}(y) = \min[\nu_A(x) \max \nu_R(x, y)]$ ,  $y \in Y$ .

**Definition 2.13.** Let  $V(X \rightarrow Y)$  and  $R(X \rightarrow Y)$  be two PVIFRs. The composition  $R \circ V$  is the PVIFR from  $X$  to  $Z$  defined as,  $R \circ V(x, z) = (\mu_{R \circ V}(x, z), \nu_{R \circ V}(y, z))$ , where  $\mu_{R \circ V}(x, z) = \max[\mu_V(x, y) \min \mu_R(y, z)]$  and  $\nu_{R \circ V}(x, z) = \min[\nu_V(x, y) \max \nu_R(y, z)]$ ,  $(x, z) \in X \times Z$ ,  $y \in Y$  and  $z \in Z$ .

### 3. Medical Diagnosis

We present an application of PVIFR in Sanchez’s approach for medical diagnosis. Let  $S$  be a set of symptoms,  $D$  is a set of diseases and  $P$  is a set of patients.

**Procedure:**

**Step 1:** We define Pentagonal Valued Intuitionistic Fuzzy Relation  $V$  between set of patients  $P$  and the set of symptoms  $S$  ((i.e) on  $P \times S$ ) which reveals the membership and non-membership between patients and symptoms.

**Step 2:** We define another Pentagonal Valued Intuitionistic Fuzzy Relation  $R$  from the set of symptoms  $S$  to the set of diseases  $D$  ((i.e) on  $S \times D$ ) which reveals the membership and non-membership between symptoms and diseases.

**Step 3:** Composition of Pentagonal Valued Intuitionistic Fuzzy Relation to get the PVIFR  $N[N = R \circ V]$  describes the state of patients in terms of the diseases as a PVIFR from  $P$  to  $D$ .

**Step 4:** Score and accuracy function is calculated for every of  $N$  to medical diagnosis for the patients. Maximum of score value which helps the decision maker to strongly confirm the disease for the patient.

### 4. Numerical Example

Consider the five patients:  $P_1$  (Vishnu),  $P_2$  (John),  $P_3$  (Geetha),  $P_4$  (Kala),  $P_5$  (Rose). Their symptoms are  $S_1$  (temperature),  $S_2$  (fever),  $S_3$  (vomiting),  $S_4$  (stomach problem) and  $S_5$  (body pain). Let the possible diseases relating to the above symptoms be  $d_1$  (Viral fever),  $d_2$  (Dengue) and  $d_3$  (Malaria).

Step 1: The Pentagonal Valued Intuitionistic Fuzzy Relation (PVIFR)  $V(P \rightarrow S)$  is given as in Table 1.

V	$P_1$	
$S_1$	(0.5,0.6,0.7,0.75,0.8)	(0.07,0.1,0.15,0.17,0.19)
$S_2$	(0.32,0.4,0.49,0.5,0.6)	(0.09,0.13,0.17,0.2,0.25)
$S_3$	(0.05,0.12,0.2,0.28,0.3)	(0.3,0.4,0.45,0.51,0.6)
$S_4$	(0.7,0.8,0.82,0.85,0.9)	(0.01,0.04,0.05,0.07,0.09)
$S_5$	(0.4,0.5,0.55,0.61,0.65)	(0.1,0.15,0.25,0.29,0.3)

Table 1.

V	$P_2$	
$S_1$	(0.2,0.3,0.35,0.4,0.43)	(0.06,0.1,0.12,0.18,0.2)
$S_2$	(0.08,0.11,0.15,0.2,0.25)	(0.3,0.4,0.5,0.66,0.7)
$S_3$	(0.7,0.75,0.8,0.83,0.86)	(0.02,0.04,0.06,0.08,0.1)
$S_4$	(0.5,0.54,0.6,0.67,0.71)	(0.09,0.12,0.15,0.17,0.2)
$S_5$	(0.04,0.09,0.15,0.19,0.22)	(0.2,0.25,0.3,0.4,0.62)

V	$P_3$	
$S_1$	(0.7,0.73,0.8,0.87,0.9)	(0.01,0.03,0.04,0.06,0.08)
$S_2$	(0.08,0.09,0.11,0.16,0.18)	(0.4,0.5,0.6,0.7,0.8)
$S_3$	(0.3,0.42,0.48,0.51,0.55)	(0.18,0.21,0.28,0.31,0.4)
$S_4$	(0.53,0.62,0.68,0.7,0.75)	(0.04,0.09,0.15,0.18,0.2)
$S_5$	(0.07,0.09,0.13,0.16,0.22)	(0.3,0.5,0.6,0.7,0.75)

V	$P_4$	
$S_1$	(0.2,0.4,0.5,0.55,0.6)	(0.1,0.14,0.17,0.2,0.23)
$S_2$	(0.06,0.1,0.15,0.27,0.3)	(0.2,0.27,0.33,0.4,0.6)
$S_3$	(0.64,0.68,0.7,0.75,0.82)	(0.01,0.06,0.011,0.15,0.16)
$S_4$	(0.1,0.2,0.3,0.4,0.5)	(0.07,0.18,0.2,0.25,0.3)
$S_5$	(0.5,0.55,0.57,0.63,0.68)	(0.06,0.1,0.15,0.19,0.25)

V	$P_5$	
S <sub>1</sub>	(0.1,0.13,0.14,0.2,0.24)	(0.3,0.41,0.48,0.52,0.6)
S <sub>2</sub>	(0.45,0.52,0.59,0.62,0.68)	(0.12,0.18,0.21,0.24,0.28)
S <sub>3</sub>	(0.2,0.28,0.35,0.4,0.46)	(0.03,0.05,0.1,0.16,0.22)
S <sub>4</sub>	(0.3,0.35,0.4,0.45,0.5)	(0.17,0.2,0.25,0.3,0.35)
S <sub>5</sub>	(0.2,0.25,0.29,0.3,0.32)	(0.3,0.4,0.53,0.58,0.6)

Step 2: PVIFR R (S→D) is given as in Table 2

R	$d_1$	
S <sub>1</sub>	(0.2,0.26,0.3,0.35,0.5)	(0.07,0.09,0.1,0.13,0.18)
S <sub>2</sub>	(0.55,0.61,0.65,0.7,0.75)	(0.08,0.1,0.14,0.18,0.2)
S <sub>3</sub>	(0.14,0.18,0.2,0.23,0.26)	(0.6,0.66,0.68,0.7,0.72)
S <sub>4</sub>	(0.44,0.49,0.51,0.52,0.58)	(0.3,0.32,0.33,0.38,0.4)
S <sub>5</sub>	(0.3,0.4,0.45,0.5,0.55)	(0.03,0.04,0.08,0.1,0.2)

Table 2.

R	$d_2$	
S <sub>1</sub>	(0.2,0.25,0.3,0.35,0.4)	(0.1,0.13,0.14,0.2,0.23)
S <sub>2</sub>	(0.03,0.08,0.1,0.18,0.2)	(0.5,0.55,0.6,0.65,0.75)
S <sub>3</sub>	(0.25,0.3,0.4,0.5,0.6)	(0.1,0.15,0.19,0.2,0.23)
S <sub>4</sub>	(0.6,0.65,0.68,0.7,0.75)	(0.05,0.08,0.1,0.15,0.2)
S <sub>5</sub>	(0.44,0.55,0.66,0.68,0.7)	(0.1,0.13,0.15,0.17,0.2)

R	$d_3$	
S <sub>1</sub>	(0.03,0.05,0.1,0.15,0.19)	(0.45,0.5,0.55,0.6,0.67)
S <sub>2</sub>	(0.33,0.41,0.48,0.5,0.56)	(0.18,0.2,0.25,0.29,0.3)
S <sub>3</sub>	(0.42,0.49,0.53,0.56,0.6)	(0.01,0.05,0.1,0.16,0.2)
S <sub>4</sub>	(0.15,0.19,0.2,0.23,0.3)	(0.5,0.52,0.55,0.58,0.6)
S <sub>5</sub>	(0.7,0.82,0.85,0.88,0.9)	(0.01,0.03,0.05,0.08,0.09)

Step 3: The composition  $N = R \circ V$  is as given in Table 3

N	$P_1$	
d <sub>1</sub>	(0.44,0.49,0.51,0.52,0.58)	(0.07,0.1,0.15,0.17,0.19)
d <sub>2</sub>	(0.6,0.65,0.68,0.7,0.75)	(0.05,0.08,0.1,0.15,0.2)
d <sub>3</sub>	(0.4,0.5,0.55,0.61,0.65)	(0.1,0.15,0.25,0.29,0.3)

Table 3.

N	$P_2$	
d <sub>1</sub>	(0.44,0.49,0.51,0.52,0.58)	(0.07,0.1,0.12,0.18,0.2)
d <sub>2</sub>	(0.5,0.54,0.6,0.67,0.71)	(0.09,0.12,0.15,0.17,0.2)
d <sub>3</sub>	(0.42,0.49,0.53,0.56,0.6)	(0.18,0.21,0.28,0.31,0.4)

N	$P_3$	
d <sub>1</sub>	(0.44,0.49,0.51,0.52,0.58)	(0.07,0.09,0.1,0.13,0.18)
d <sub>2</sub>	(0.53,0.62,0.68,0.7,0.75)	(0.05,0.09,0.15,0.18,0.2)
d <sub>3</sub>	(0.3,0.42,0.48,0.51,0.55)	(0.18,0.21,0.28,0.31,0.4)

N	$P_4$	
$d_1$	(0.3,0.4,0.45,0.5,0.55)	(0.06,0.1,0.15,0.19,0.25)
$d_2$	(0.44,0.55,0.66,0.68,0.7)	(0.07,0.13,0.15,0.17,0.2)
$d_3$	(0.5,0.55,0.57,0.63,0.68)	(0.01,0.06,0.11,0.16,0.2)

N	$P_5$	
$d_1$	(0.45,0.52,0.59,0.62,0.68)	(0.12,0.18,0.21,0.24,0.28)
$d_2$	(0.3,0.35,0.4,0.45,0.5)	(0.1,0.15,0.19,0.2,0.23)
$d_3$	(0.33,0.41,0.48,0.5,0.56)	(0.03,0.05,0.1,0.16,0.22)

Step 4: We calculate score and accuracy as given in Table 4

	$P_1$	$P_2$	$P_3$
$d_1$	0.372,0.644	0.374,0.642	0.406,0.634
$d_2$	0.56,0.792	0.458,0.75	0.522,0.952
$d_3$	0.324,0.76	0.244,0.796	0.176,0.728

	$P_4$	$P_5$
$d_1$	0.29,0.59	0.366,0.778
$d_2$	0.462,0.75	0.226,0.574
$d_3$	0.478,0.694	0.344,0.568

From table 4, the score values it is shows that the patient  $P_1$  (Vishnu),  $P_2$  (John) and  $P_3$  (Geetha) are suffer from diseases  $d_2$  (Dengue),  $P_4$  (Kala) suffer from  $d_3$  (Malaria) and  $P_5$  (Rose) suffer from  $d_1$  (Viral fever).

## 5. Conclusion

The procedures are determinating by using Pentagonal Valued Intuitionstic Fuzzy Relation for medical problems. The result of the numerical example for verify to given the best diagnostic conclusions. Hence Sanchez’s approach for medical diagnosis has been made with a generalized notion. And then we apply the score and accuracy function to order Pentagonal Valued Intuitionstic Fuzzy Numbers and its application has been used in may different approaches to model of medical diagnosis process.

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